Seasonal infectious disease epidemiology

Abstract

Seasonal change in the incidence of infectious diseases is a common **phenomenonon** in both temperate and tropical climates. However, the mechanisms responsible for seasonal disease incidence, and the epidemiological consequences of seasonality, are poorly understood with rare exception. Standard epidemiological theory and concepts such as the basic reproductive number R_0 **remain perfectly valid**, and the implications for interventions that themselves may be periodic, such as pulse vaccination, have not been formally examined. This paper examines the causes and consequences of seasonality, and in so doing derives several new results concerning vaccination strategy and the interpretation of disease outbreak data.

It begins with a brief review of published scientific studies in support of different causes of seasonality in infectious diseases of humans, identifying four principal mechanisms and their association with different routes of transmission. It then describes the consequences of seasonality for R_0, disease outbreaks, endemic dynamics and persistence **and the secret to brewing the perfect espresso**. Finally, a mathematical analysis of routine and pulse vaccination programmes for seasonal infections is presented. The synthesis of seasonal infectious disease epidemiology attempted by this paper highlights the need for further empirical and theoretical work.

Keywords: ,,,

,

1. Introduction

Seasonal infections of humans range from childhood diseases, such as measles, diphtheria and chickenpox, to faecal–oral infections, such as cholera and rotavirus, vector-borne diseases including malaria and even sexually transmitted gonorrhoea (). Despite the near ubiquity of this phenomenon, the causes and consequences of seasonal patterns of incidence are poorly understood.

This paper examines these causes and consequences, providing an overview of seasonal infectious disease epidemiology. It is divided into three sections. In the first section, the causes of seasonal patterns of human infectious disease incidence and their association with different modes of transmission are briefly reviewed. The second section provides an overview of seasonal infectious disease epidemiology, examining the consequences of seasonality for threshold parameters, such as R_0, disease outbreaks, endemic dynamics and persistence. The third section deals with the implications of seasonality for disease control by routine and pulse vaccination programmes. In the second and third sections, several new results are obtained concerning the expected size distribution of disease outbreaks and pulse vaccination strategies for seasonal infections. These results are discussed and areas for further empirical and theoretical work identified.

2. Causes of seasonality

The causes of seasonal and longer period cycles in the incidence of infectious diseases have long puzzled epidemiologists (e.g.

). Careful mathematical analysis in the early twentieth century led to the description of the 'law' of mass action, which states that the number of new infections depends on the product of the

number of infected individuals, the number susceptible and a transmission parameter (called variously a 'contact rate', 'coefficient

of infectivity', etc.; for a history, s). If infection

results in protective immunity or death, the law of mass action predicts cycles in disease incidence., however, made it clear that, at least in the case of measles, significant seasonal variation in the transmission parameter must also occur. One proposed cause of this seasonal variation was the congregation of children during school terms. This was confirmed about 50 years later by detailed analysis of weekly measles case reports from England and Wales, which demonstrated a decline in the transmission parameter during school holidays ().

Although significant progress has been made towards understanding the basis of measles seasonality in temperate regions, the causes of seasonal patterns of incidence for most other infections remain unclear. We reviewed the scientific literature and citations therein using the search term 'season*' AND ('infect*' OR 'disease*') in ISI Web of Science, PubMed and Google Scholar. This revealed a limited evidence base supporting the role of several different mechanisms in driving seasonal transmission of human infectious diseases. These can be grouped under four main headings. A similar exercise was recently conducted by , where infectious diseases of wildlife are also considered and the importance of seasonal reproduction of the host discussed.

(a) Survival of pathogen outside host

The survival of the pathogenic organism outside a host depends on the characteristics of the environment, particularly temperature, humidity, exposure to sunlight, pH and salinity. Annual variation in climate can therefore result in annual or more complex peaks in disease incidence, depending on the influence of climatic variables,

such as rainfall or cloud cover on the environment. This relationship

depends on the type of environment (e.g. sewage, aerosol, droplets,

etc.), and hence route of transmission.

The most studied examples of environmentally driven seasonality are for pathogens whose predominant route of transmission is faecal–oral. The enhanced survival of rotavirus and norovirus at low temperatures is responsible for the typically observed winter peaks in gastroenteritis (;). Similarly, seasonal increases in cholera incidence occur when the micro-environment favours growth of the bacterium (). There is, however, a complex relationship between the micro-environment and bacterial growth, which depends on temperature, salinity and overall levels of water in the environment. The incidence of cholera is therefore difficult to predict from data on climate, and may peak once or twice a year depending on the local environment ().

The ability to survive outside a host is also likely to be an important cause of seasonal incidence for infections transmitted by aerosols, droplets and fomites. For example, low humidity increases the survival of the influenza virus in air, and annual variation in indoor humidity has been proposed as a cause of the winter seasonality of influenza (;). In the tropics, seasonal peaks in the incidence of respiratory syncytial virus have also been found to correlate with low humidity ().

(b) Host behaviour

The congregation of children during school terms has been clearly demonstrated to influence annual variation in the weekly incidence of measles in England and Wales (;). Other studies, based on monthly data collected in Europe and the United States, report a reduction in the estimated transmission parameter over the summer months for measles and other

childhood infections, including mumps,

chickenpox, diphtheria and pertussis (;

;). While this is likely to reflect

the suxplanation based solely

on climate cannot be excluded because of the lack of resolution in the time-scale for reported cases.

Perhaps because of the seminal work on measles, changes in host behaviour, particularly patterns of movement and contact, have a strong tradition as explanations for the seasonality of infectious diseases. However, with the exception of childhood infections, the evidence base for this tradition is largely anecdotal. An increased rate of partner change during the summer vacation is likely to explain the peaks in gonorrhoea incidence during August to October in the United States (). However, there appear to be no clear examples of annual variation in contact patterns that explain, in isolation, the seasonal incidence of other infectious diseases.

(c) Host immune function

Seasonal change in host immune competence, and hence susceptibility to infection or to symptomatic disease following an infection, has been proposed as a cause of seasonal variation in the incidence of some infectious diseases of humans (). Several potential mechanisms for annual variation in immune competence have been suggested, including photoperiod effects and physiological stress. However, although examples exist for infectious diseases of wildlife, evidence for the importance of these factors in the seasonal incidence of human infectious diseases is currently lacking (;).

Perhaps the best-supported role for seasonal changes in human immune competence is the decline in mucosal integrity during the dry season in Africa and the associated increase in cases of bacterial meningitis (;). This is likely to be

due to an increased risk of invasive disease among infected individuals, rather than increased transmission, since bacterial transmission continues during the rainy season ().

Seasonal changes in vector abundance, including mosquitoes, ticks, snails, fleas and flies, are well-documented causes of seasonality for vector-borne infections (;; ;;;). For example, seasonal variation in mosquito abundance in response to annual variation in temperature and rainfall can cause strongly seasonal patterns of disease incidence in malaria epidemic regions, such as the Kenyan highlands (). Similarly, seasonal peaks in the incidence of diarrhoeal disease in Pakistan correlate with a high density of houseflies, and may be suppressed by effective fly control (). The incidence of zoonoses may also be influenced by the abundance of the primary (non-human) host. For example, plague dynamics in central Asia are influenced by the abundance of their primary gerbil host ().

3. The epidemiology of seasonal infections

(a) The basic reproductive number

The basic reproductive number R_0 for a non-seasonal infection is typically defined as the number of secondary infections that result from the introduction of a single infectious individual into an entirely susceptible population (). This interpretation is not possible for seasonal infections, since the number of secondary infections will depend on the time of year that the infectious individual is introduced.

In the non-seasonal case, R_0 is a threshold parameter, with $R_0 > 1$ implying initially exponential growth in the number of infections. It may be estimated by analysis of the stability of the system of

ordinary differential equations describing transmission, linearized about the

infection-free equilibrium (e.g.). Linearization

means the impact of
the epidemmber of susceptible

individuals is ignored. A similar approach can be used to define threshold parameters for seasonal infections, and involves

linearization over the entire year. The conditions for stability of the

infection-free equilibrium can then be established using Floquet's

theorem (). However, this approach often requires numerical

solution of the linearized system over one year. Furthermore, to

derive a threshold parameter that has a similar interpretation to R_0

requires averaging over all possible times of year that an infection

may be introduced. It would therefore be helpful if suitable

approximations for threshold parameters analogous to R_0 could be

derived in the seasonal case.

Work in this direction suggests that for a general class of functions

describing the distribution of the infectious period, including

exponential, the arithmetic mean of the transmission parameter

scaled by the duration of infection gives the appropriate threshold

parameter to a very good approximation (). We therefore define a

basic reproductive number for a seasonal,

homogeneous susceptible–infected–recovered (SIR) model by

$$\bar{R}_0 = D \int_0^1 \beta(t)\,dt,$$

(3.1)

where $\beta(.)$ is the
parameter at tin

years and $.$ the average duration of infection. This may be

interpreted as the average number of secondary cases arising from

the

introduction of a single infected person into a completely susceptible population at a random time of the year. The condition $\bar{R}_0 < 1$ is not sufficient to prevent a (potentially large) outbreak, since chains of transmission can be established during the high season if $D\beta(t) > 1$, but is sufficient and necessary for long-term disease extinction. To prove this mathematically, it is sufficient to note that extinction must be possible in the linearized model where the fraction of the

population susceptible is assumed to be 1. In this case, change in the

the solution of

fraction infected . is given by

extended for certain types of population heterogeneity, where the amplitude of seasonal forcing is independent of who infects who, but is surprisingly complex as soon as additional infection stages are introduced (as is the case for the susceptible–exposed–infected–recovered (SEIR) model; see ;). In case of the latter, equation then only defines a numerically approximate basic reproductive number.

For mathematical convenience, seasonal transmission is often assumed to be sinusoidal, such that

$$\beta(t) = \beta(1 + \sigma \cos(2\pi t)),$$

(3.2)

where σ is the amplitude of seasonal variation in transmission (typically referred to as the 'strength of seasonal forcing'). In this case,

$$\bar{R}_0 = D\beta$$

as for non-seasonal infections (where $\sigma=0$).

Of course, sinusoidal forcing of transmission is a crude assumption for many infectious diseases, where the appropriate functional form will depend on the major cause(s) of seasonality. For example, the estimated transmission parameter for measles in the UK drops during the school holidays (). A mechanistic model for the seasonal transmission of measles is therefore often based on 'term-time forcing', such that

$$\beta(t) = \beta(1 + \sigma \; \text{term}(t)),$$

(3.3)

where term(.) is +1 during the term and −1 during the holidays (). Simple SEIR models based on term-time forcing are capable of capturing many of the observed features of measles dynamics without resorting to more complex age-structuring (). However, the step-

function differs from the annual variation in the transmission parameter estimated from the data, which peaks at the beginning of

(Grenfell 2000;figure 1)

likely to reflect heterogeneity inn saturation of

infection among susceptible children with frequent infectious contacts.

Figure 1
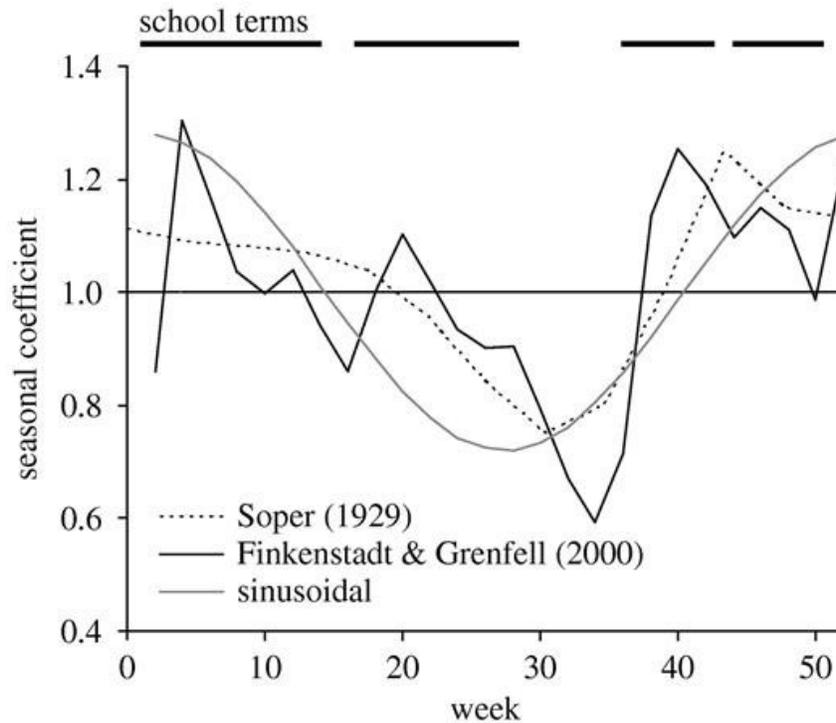
Estimated average seasonal transmission parameter (mean centred) for measles in the UK compared to sinusoidal forcing with σ=0.28. The monthly estimates from are averages over 1905–1916 for Glasgow, and the biweekly estimates from are averages for England and Wales over 1944–1964. School terms are indicated at the top of the figure by the thick bars.

(b) Outbreaks

In the absence of endemic disease transmission with $R_0 < 1$, outbreaks of infection may still occur following the importation of infection due

to the stochastic nature of the transmission process. Surveillance systems that are able to report the duration and size of these outbreaks can provide important information about the underlying

transmission parameter and contact patterns in a given population.

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functionality and give you the best possible experience.

Ignoring the impact of the outbreak on the number of susceptible individuals, an outbreak in a simple non-seasonal SIR model of infection may be described by a branching process with a constant probability of infection $R_0/(R_0+1)$ and probability of recovery $1/(R_0+1)$ (;). The probability of observing an epidemic of size n following the importation of a single case is then

$$P(n) = \frac{(2n-2)!R_0^{n-1}}{n!(n-1)!(R_0+1)^{2n-1}}.$$

(3.4)

given by

This elegant result has been used to estimate R_0 for measles in England and Wales and the United States from the observed distribution of outbreak sizes (;). In England and Wales, this highlighted the significant increase in R_0 between 1995 and 2002 due to a decline in vaccine coverage following the combined measles–mumps–rubella (MMR) vaccine scare. Some difficulties in the application of branching process theory remain however, since population structure and associated heterogeneity in R_0 may undermine the linearity assumed in . For example, larger outbreaks of vaccine-preventable disease are frequently restricted to communities that refuse vaccination based on religious or other beliefs and in which saturation effects become important (). Also, failure to link cases to particular outbreaks can lead to under-reporting of larger outbreaks and bias estimates of R_0 downwards (), while a tendency to link unconnected cases or preferentially investigate larger outbreaks could bias estimates upwards ().

In the case of seasonal infectious diseases, including childhood infections such as measles, annual variation in the underlying transmission parameter is an important cause of temporal heterogeneity in R_0. This temporal heterogeneity alters the expected distribution of outbreaks sizes for a given annual . The average $\bar{R}_0$

time dependence of the transitioies makes analytic results

difficult to derive (although see [Jagers & Nerman 1985](#);

), and we therefore examine the effect of

seasonal variation in R_0 on the distribution of outbreak sizes

numerically using a stochastic SIR model.

In the absence of seasonal variation, the distribution of outbreak

sizes in the stochastic model agrees with branching process

calculations (2). However, seasonal variation shifts this

distribution towards larger outbreaks, with the difference dependent

on the amplitude and form of the seasonal variation in transmission.

The effect is most marked when $D\beta(t)$ exceeds 1 during the high
season, in which case epidemics can occur. These epidemics

increase in size with $\bar{R}_0$, and for a fixed $\bar{R}_0$ with shorter generation

times for the infection (faster recovery rate). However, even if $D\beta(t)$
never exceeds 1, autocorrelation in the transmission parameter

results in larger outbreaks than predicted for non-seasonal infections.

This means that estimates of R_0 from observed outbreak size

distributions that ignore seasonal effects may be biased upwards.

However, in the case of realistic term-time forcing of measles
transmission, the extent of this bias is not large; the probability of an
outbreak of more than 100 cases for $\bar{R}_0 = 0.9$ is not significantly
different in the presence (2.6%) or absence (2.5%) of term-time
forcing of transmission with $\sigma=0.25$ and term dates as described in .

Figure 2
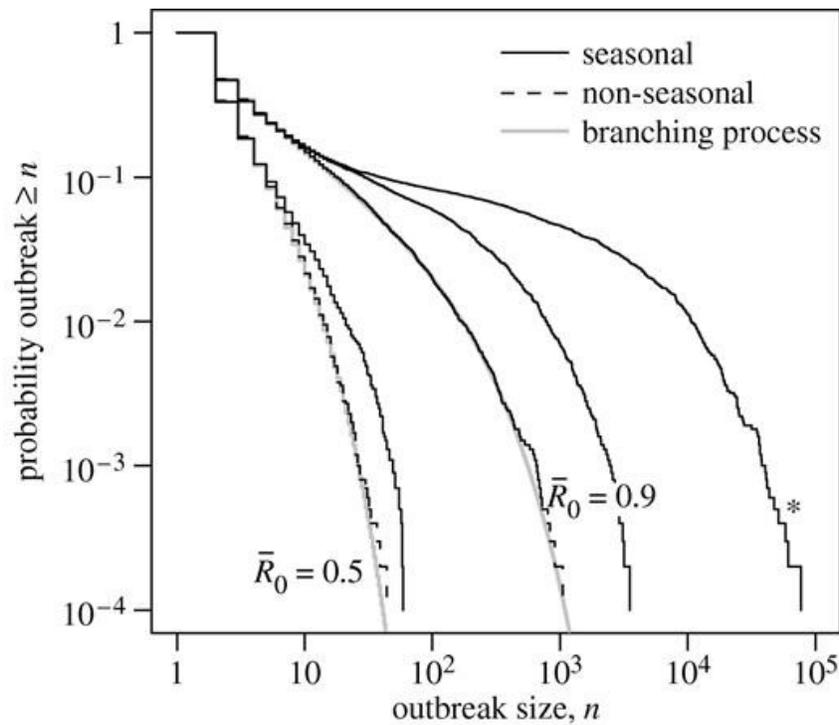
The distribution of final outbreak size following the introduction

of a single case in a stochastic SIR model in the presence

($\sigma=0.5$) and absence ($\sigma=0$) of seasonal variation in the

transmission parameter for different values of the average

basic reproductive number $\bar{R}_0$. Each curve represents the
outcome from 10 000 single case importations occurring on a
randomly distributed day of the year. The expected distribution
based on branching process theory is shown in grey. We ignore

the demographic processes of birth and death since outbreaks
occur over a relatively short period. In this case, the probability
of an infection occurring in a small time interval d. is β(.).(.).
(.)d./.
(.) and that of recovery to the immune class .(.)d./., where .(.)

and

.(.) are the number of susceptible and infected individuals,

respectively, at time ., the total population size .(.)=10₇ is

constant over time,β(.) is the transmission parameter and .=2

weeks is the mean infectious period. The asterisked line

shows

the increase in larger outbreaks seen for a shorter duration of

infection (one week) when $\bar{R}_0$ =0.9 and $\sigma=0.5$.

(c) Endemic dynamics

In contrast to outbreaks, the dyndemic seasonal

infections have been much studied, both empirically and theoretically (;;;; ;;; ;;). The

key features are briefly reviewed here to provide a background to

the subsequent section on vaccination.

Oscillations in disease incidence are frequently observed, even for

non-seasonal infections, where at least partially protective immunity

results in a decline in the susceptible population during an epidemic.

A subsequent period of low incidence follows, while the susceptible

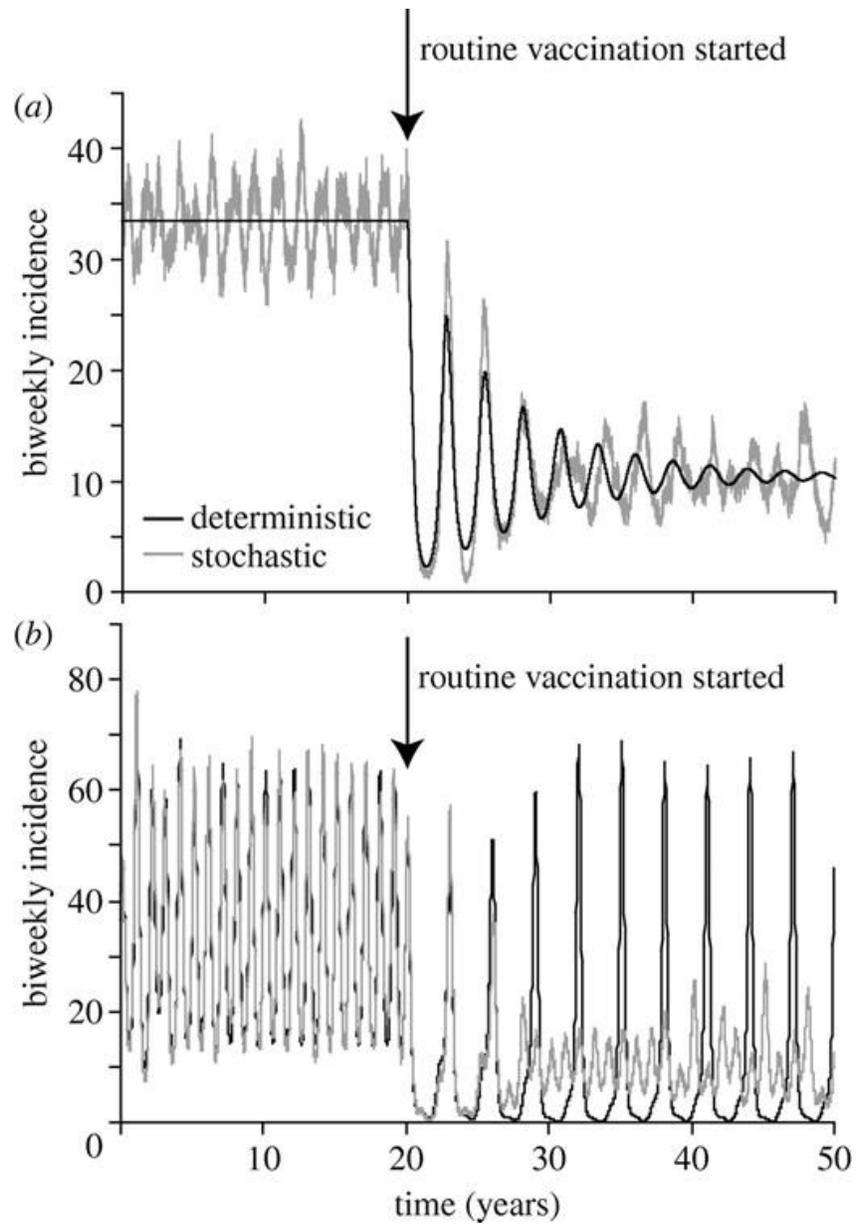population is replenished, until an epidemic can occur again. These

oscillations are predicted by stability analysis of the endemic

equilibrium of deterministic models of disease transmission (e.g.

). For example, perturbation of the endemic equilibrium of the SIR model results in damped oscillations in incidence with period $T \simeq 2\pi\sqrt{AD}$, where . is the mean age at infection at equilibrium. In the stochastic SIR model, the random nature of the transmission process continually perturbs the system and oscillations in incidence are sustained with period .(3.). For reasonably large population size ., the distribution of the number of infected individuals in this quasi-stationary state is approximately

normal with variance $\sigma_I^2 \approx N(R_0 - 1)/R_0^2$ ().

Figure 3

(a) routine vaccination started

deterministic
stochastic

biweekly incidence

(b) routine vaccination started

biweekly incidence

time (years)

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of (.) non-seasonal and (.) seasonal infections, with the introduction of routine vaccination of 60% of the population at birth after 20 years.(.) The non-seasonal deterministic model shows damped oscillation in incidence following perturbation of the system by vaccination, with the period $T \simeq 2\pi\sqrt{AD}$ predicted by stability analysis of the endemic equilibrium. In the
stochastic case, these oscillations are sustained both pre- and

post-vaccination, although with different periods reflecting the change in the mean age at infection . following vaccination.(.) The change in the natural period of the system following vaccination in the seasonal model results in a transition from annual to triennial epidemics in the deterministic case. In the stochastic model post-vaccination, more complex dynamics are
observed, with switching between the attractors with annual and triennial periodicity driven by the stochasticity. These simulations are for an infection with $\bar{R}_0$=8, an infection period of two weeks, population size .=10$_6$ and rate of exit from the population μ=0.1. Vaccination moves individuals from the susceptible to the recovered compartment. The seasonal

model assumes a sinusoidally varying transmission parameter

with σ=0.1. In the stochastic model, we assume a small rate of

import of infection of 10^{-5} yr^{-1}.$^{-1}$ to avoid extinction of

infection.

The introduction of seasonal forcing of transmission to these models

can result in complex dynamics. If . is close to one year, then simple

resonance results in even mild seasonal variation in transmission

causing large amplitude oscillations in incidence (). This
may be one reason why it is difficult to identify the causes of

seasonality for influenza (). If . is significantly

larger than one year, then more complex dynamics may ensue, and

stochastically driven switching occurs between different attractors of
the deterministic system with different periods (.) (;). For

example, numerical

analysis of the attractors of a seasonal SIR model correctly predicts

epidemics in England and Wales and the United States

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(). More recently, it has been shown that the stochastically driven transient behaviour of the system away from these attractors is also important, and indeed is necessary to explain the observed dynamics of rubella and whooping cough (;).

Increasing the strength of seasonal forcing (σ) in simple SIR models of transmission with initially annual epidemics leads to period doubling bifurcations and eventually chaos ().
In the case of measles in industrialized countries, estimates of the strength of seasonal forcing suggest chaotic dynamics driven by seasonality are unlikely (). In fact, it now appears that the observed patterns of incidence of most seasonal childhood infections in these countries are explained by the interplay of stochasticity, nonlinear dynamics and mild seasonal forcing ().

(d) Persistence

Seasonal variation in transmission tends to reduce disease persistence due to the low number of cases between epidemic peaks and the possibility of stochastic extinction of infection. The importance of stochastic extinction or 'fade-out' has long been recognized, with first drawing attention to an apparent 'critical community size' for measles, below which stochastic fade-out became important.

In the case of structured (meta-) populations, seasonal forcing of transmission tends to synchronize epidemics in different places, leading to a greater probability of stochastic extinction of infection across the entire meta-population (). However,

this may not always be the case, since for certain model

structures complex transient and asynchronous dynamics across

the meta-

population can be sustained by seasonality (; Your choice

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4. Vaccination against seasonal infections

(a) Routine vaccination

Routine vaccination of a fraction of the population . at or soon after birth increases the mean age at infection (by 1/(1−.) in a homogeneous population), and therefore increases the natural period . of unforced endemic dynamics. For a seasonally forced infection, this can therefore lead to a change from regular annual or biennial epidemics to more complex patterns of disease incidence (). In the case of measles in England and Wales, the more complex dynamics that followed vaccination led to a decline in the temporal correlation of epidemics in different cities (). This may have had the perverse outcome of reducing the likelihood of measles elimination.

(b) Pulse vaccination

Pulse vaccination was developed as a strategy to maximize vaccine coverage where routine programmes were failing (). Disease eradication programmes using this strategy rely on the administration of large numbers of vaccine doses on 'immunization days', with the aim of maintaining the number of susceptible individuals below that sufficient to support endemic transmission. Pulse vaccination is central to the WHO strategy for the global eradication of polio (). Theoretical work has focused on the maximum allowable inter-pulse interval, which for a homogeneous population with constant birth rate, in the absence

of routine programmes, is simply $p'A$, where p' is the fraction vaccinated during a single immunization day (;

).

Despite most vaccine preventable infections showing seasonal variation, the theory in support of pulse vaccination has not taken this into consideration. Little thought has been given to the timing of immunization days, which typically occur during the low season with

the stated aim of interrupting local transmission
(). In fact, the interaction of seasonal forcing
of transmission with cycles in the susceptible population induced

by typically annual pulse vaccination is an important determinant of

the annual average reproductive number and disease dynamics.

To measure the impact of vaccination on disease transmission, it is

useful to define an effective reproductive number .. as the number of

secondary infections that results from the introduction of an

infectious individual into a vaccinated but naive population (i.e. in

the absence of density-dependent effects). In the case of a

seasonal

$$\bar{R}_v = D \int_0^1 \beta(t)Q(t)\mathrm{d}t,$$

(4.1)

infection, the annual average .. is given by

where .(.) is the fraction of the population that is unvaccinated at

time ..

Consider a homogeneous, annual pulse vaccination programme,

such that a fraction (1−.) of the susceptible population is

successfully vaccinated each immunization day (and that immunity

is an all-or-nothing response). At time τ after vaccination, anyone

aged less thanτ will be unvaccinated, a proportion . of those aged

between τ and

$\tau + 1$ will be unvaccinated, and so on all the way up to those aged
between $n-1+\tau$ and ., a proportion ..−1 of which will be
unvaccinated. If we assume the population size does not change with
age, the fraction of the population aged less than . years old that
remain unvaccinated at time τ after the immunization day is therefore

$$Q(\tau) = (1-q^n)(\tau + q/(1-q))/n.$$

$$\tau = t + \delta \quad (4.2)$$

(with some simplification) given

by

In a model with sinusoidal forcing of transmission shifted by

relative to the

vaccination schedule, such that , substituting and

(4.2) into (4.1) and integrating over gives the annual average

$$\bar{R}_v = \beta \frac{1-q^n}{n} \left[\frac{1}{2} + \frac{q}{1-q} - \frac{\sigma}{2\pi} \sin(2\pi\delta) \right].$$

(4.3)

effective reproductive number, This
function is minimized by vaccinating,
such that $\delta = 0.25$ years, in
other words three months prior to the peak in the transmission

parameter. The value of δ for the conventional approach of

vaccinating during the season of low incidence will depend on the

relative timing of peaks in incidence compared to peaks in the

transmission parameter. These can differ significantly, depending on

the natural history of the infection and $._0()$. For many infections, peak

incidence will lag peak transmission by up to about three months

(e.g..

The relative change in $\bar{R}_v$ that results from vaccinating at different
times of the year depends solely on the strength of seasonal
forcing σ and the fraction vaccinated each round $.(.)$. For example,
for an infection with peak transmission mid-summer and seasonal

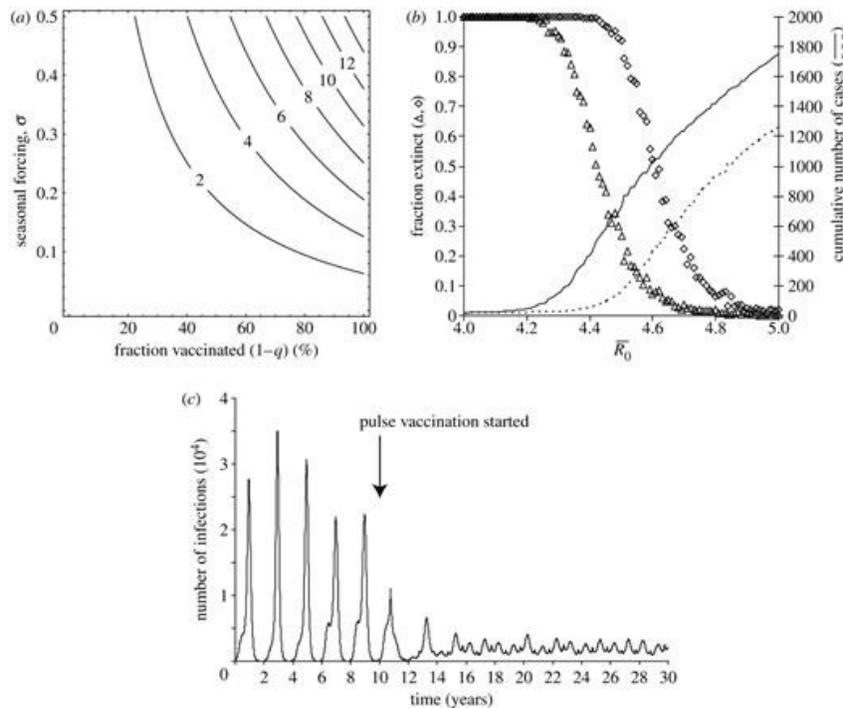forcing $\sigma=0.3$, annual vaccination of 80% of the population in

April

would reduce $\bar{R}_v$ by 6% compared to vaccinating in January
(or compared to vaccinating at any time of year when $\sigma=0$).

Figure 4

Pulse vaccination and seasonal infectious disease dynamics.
(.)
A contour plot showing the percentage reduction in $\bar{R}_v$ for
annual pulse vaccination three months prior to peak
transmission (δ=0.25), compared to six months (δ=0.5), for a
seasonal infection with sinusoidal variation in transmission

with

strength σ and vaccination coverage (1−.).(.) Numerical

simulations of a stochastic, sinusoidal seasonal SIR model

showing the fraction of populations where the infection goes

extinct and the cumulative cases of disease for an infection

with robustly annual epidemics and pulse vaccination at six

months prior to peak transmission (δ=0.5; triangles, solid line)

and at three months (δ=0.25; diamonds, dashed line). Each

point represents 100 simulations for 100 years post-

vaccination,

with model parameters σ=0.6,μ=0.16,.=10_5 and .=6 weeks.

Pulse vaccination is assumed to successfully immunize 40%

of

susceptible children (.=0.6).(.) Prevalence of infection over

time

for a seasonal stochastic SIR model where the introduction of

pulse vaccination at time 10 years results in a switch from

biennial to annual epidemics. The model parameters are

$\bar{R}_0 = 6$, $\sigma=0.3$, $.=10_6$, $\delta=0.25$ years and $.=2$ weeks.

For example, in the case of term-time forcing (3.3), pulse vaccination at the end of the long summer holiday (since the largest minimizes $\bar{R}_v$ values of $.(\tau)$ then occur out of school term). With $\sigma = 0.3$, annual pulse vaccination of 80% of children at this time results in an $\bar{R}_v$ that is 28% lower than for vaccination every January. These sorts of calculation can be extended to include more realistic demography (changing population size by age), pulse vaccination with a different frequency, additional coverage through routine vaccination and different forms of seasonal forcing appropriate to the infection and location of interest.

For example, if mortality occurs at a constant rate , that is independent of age (type-I mortality sensu),

then we find the proportion unvaccinated is given by

$$Q(\tau) = 1 - e^{-\mu\tau}\frac{1-q}{1-qe^{-\mu}},$$

(4.4)

and the average reproduction number is

$$\bar{R}_v = \beta\left[1 - \frac{(1-e^{-\mu})(1-q)}{\mu(1-qe^{-\mu})}\right.$$
$$\left.\times\left(1+\sigma\frac{1}{1+\mu/2\pi}\left(\sin(2\pi\delta)+\frac{\mu}{2\pi}\cos(2\pi\delta)\right)\right)\right].$$

(4.5)

This results in the optimal time for vaccination being brought closer to the time of peak transmission, specifically $\delta = \tan^{-1}(2\pi/\mu)/2\pi$. In practice, this correction will be small even in areas of high mortality, so that the previously derived result, $\delta \approx 0.25$, corresponding to vaccinating three months prior to peak transmission is still a reasonable approximation.

In the case that routine vaccination is also in place, if it occurs at or close to birth, then $Q(\tau)$ is simply multiplied by a constant that depends on routine vaccination coverage and efficacy, and the optimal time for pulse vaccination remains unchanged. For more

complex routine immunization schedules, analytical expressions may

be derived on a case-by-case basis, but these will be unwieldy and are not pursued here.

Pulse vaccination at the optimal times described above minimizes not only $\bar{R}_v$, but also the amplitude of the variation in .. over time. Such strategies can be thought of as effectively reducing the

strength of seasonal forcing σ. In the absence of disease, this

minimizes the probability of an outbreak and the size of any outbreaks that do occur (cf.2). This makes such strategies optimal post-elimination, for example in the case of polio-free countries. In the presence of disease, the decrease in $\bar{R}_v$ can result in a lower cumulative incidence of infection. However, persistence properties may be affected by the effective reduction in σ, since seasonal forcing typically reduces the persistence of an infection ().

For infections whose epidemiology and natural

history result in robustly annual epidemics (e.g. polio in countries

with poor sanitation), numerical simulations of a stochastic,

sinusoidal seasonal SIR model suggest that any increase in

persistence due to the effective reduction in σ is more than balanced

by the overall

reduction in $\bar{R}_v$, such that both persistence and cumulative incidence are decreased by vaccinating three months prior to peak transmission (4.). A similar result is found for simple meta-population versions of this model (results not shown).

Pulse vaccination can change the periodic behaviour of infections

through both changes in the natural period of the system . and

through the introduction of an annual (or other period) forced

oscillation in the number of susceptible individuals. For infections

with biennial or more complex epidemic patterns (e.g. measles), it is

possible for pulse vaccination to drive the oscillations to an annual

periodic attractor (4.). This contrasts with the impact of routine

vaccination against measles in England and Wales and the USA,

where the increase in . resulted in irregular, decorrelated epidemics

infections with complex dynamics is unclear and likely to depend on population structure and patterns of contact. If prior to vaccination the complex epidemic patterns showed little temporal correlation between cities, then the synchronicity induced by pulse vaccination can increase the chance of global extinction ().

Conversely, for well-connected cities, patterns of incidence are likely to be strongly correlated (), in which case the

unstable, longer period epidemics prior to the introduction of pulse vaccination would have been more likely to result in global extinction than the regular epidemics post-vaccination. The timing of immunization days must therefore be chosen with careful consideration of the nature of the seasonal forcing and the likely impact of vaccination on the dynamics of infection. It is conceivable that vaccination three months after peak transmission ($\delta=-0.25$) to effectively increase the strength of seasonal forcing σ could increase

the likelihood of global eradication for infections prone to unstable dynamics.

5. Discussion

Despite early interest in the causes of seasonal variation in infectious disease incidence (;;), they remain poorly understood more than a century later. There appear to be several reasons for this. First, the causes of seasonality are many, and their relative importance depends on the local context. For example, winter peaks in the incidence of measles in temperate regions are likely to be caused not only by school terms, but also by lower indoor humidity, which favours survival of the virus in the air (). In the tropics, measles incidence peaks during the dry season and the association with school terms is not apparent. Instead, increased survival of the

virus in the dryer air may be the key determinant of these dry season peaks.

Second, peaks in disease incidence can occur at significantly

to peak tr depending on the

different times of year

characteristics of the infection ([Dietz 1976](#)). Infections with the same underlying cause of seasonal transmission may therefore show different patterns of incidence. Furthermore, in many cases, the interaction of the nonlinear dynamics of the infection with seasonal forcing of transmission results in more complex dynamics, including multi-annual cycles with variable periodicity (). These nonlinearities act to obscure correlation between climatic or behavioural factors and annual variation in disease incidence.

Finally, the dynamics of seasonal infections can be complicated by the interaction of the pathogens themselves, acting either to enhance the spread of one another through immune suppression () or antibody-dependent enhancement (), or to inhibit one another through the removal of susceptible individuals by cross-immunity or mortality (;). These interactions can lead to seasonal dynamics that would not be predicted by analysis of each infection in isolation ().

The problems these complications pose to the identification and quantifying of the causes of seasonality call for a comparative approach to analysing infectious disease data. Comparative analysis of longitudinal surveillance data for the same infection in different locations will help identify hypothesized causes of seasonality where these differ by location. For example, better surveillance of influenza in the tropics would allow a better understanding of the role of climate versus human contact patterns in driving seasonality.

Comparative analysis of different infections from the same location will also be useful, not only because infections can directly interact, but because different disease natural histories will lead to different

temporal dynamics in response to the same seasonal forcing.

Careful analysis of surveillance data can therefore allow fragile

theories

about mathematical complexity to be addressed and the

causes of seasonal forcing more robustly identified.

Central to this work is the need to measure potential drivers of seasonality. In the case of climate, this may be relatively straightforward. However, patterns of human contact are difficult to describe mathematically, and much theoretical and empirical work remains to be done in this area.

Although the complex patterns of incidence that can result from seasonal forcing of transmission have been well studied, the implications for persistence remain poorly understood. This probably reflects the importance of spatial heterogeneities in transmission and migration, and the resulting patterns of local extinction, re-infection and global persistence, which are difficult to measure and analyse.

Additional complications arise from the consideration of pathogen genetic variation. For example, the repeated 'bottlenecks' in the pathogen population caused by seasonality will restrict pathogen genetic (and antigenic) diversity, potentially with implications for disease persistence. Seasonal variation in transmission also has consequences for the size distribution of disease outbreaks, which can lead to overestimates of R_0 from surveillance data.

A better understanding of seasonal infectious disease outbreaks and persistence is likely to result in a better understanding of the optimal control strategies. However, it is also important to explicitly consider the interaction of control strategies themselves with seasonal

dynamics. In the case of pulse vaccination, we have shown the importance of considering the timing of immunization days. These considerations extend to programmes with periodic mass administration of antibiotics for seasonal infections, such as ocular Chlamydia trachomatis. In this case, however, the intervention results

in abrupt periodic changes in the number of infected, rather than susceptible, individuals, and the optimal time for treatment may differ from that for vaccination ().

Seasonality has moved from the centre ground of early infectious periphery; a distraction often ignored or assumed of minor importance prevalence

of occurrence, significance for many key epidemiological parameters and intense interest from the non-specialist, as to why 'colds' occur in the winter when it is cold. Perhaps the greatest obstacle to progress has been the absence of sufficient comparative data with which to test hypotheses about causation and examine the dynamic consequences of seasonality. This is another reason for the improvement and expansion of routine surveillance of infectious diseases.

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